

Neutralino dark matter and collider signals with and without soft term universality

Eun-Kyung Park
Bonn University

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in collaboration with

H. Baer (Florida State U., U. of Oklahoma), A. Mustafayev (U. of Kansas) and X. Tata (U. of Hawaii)

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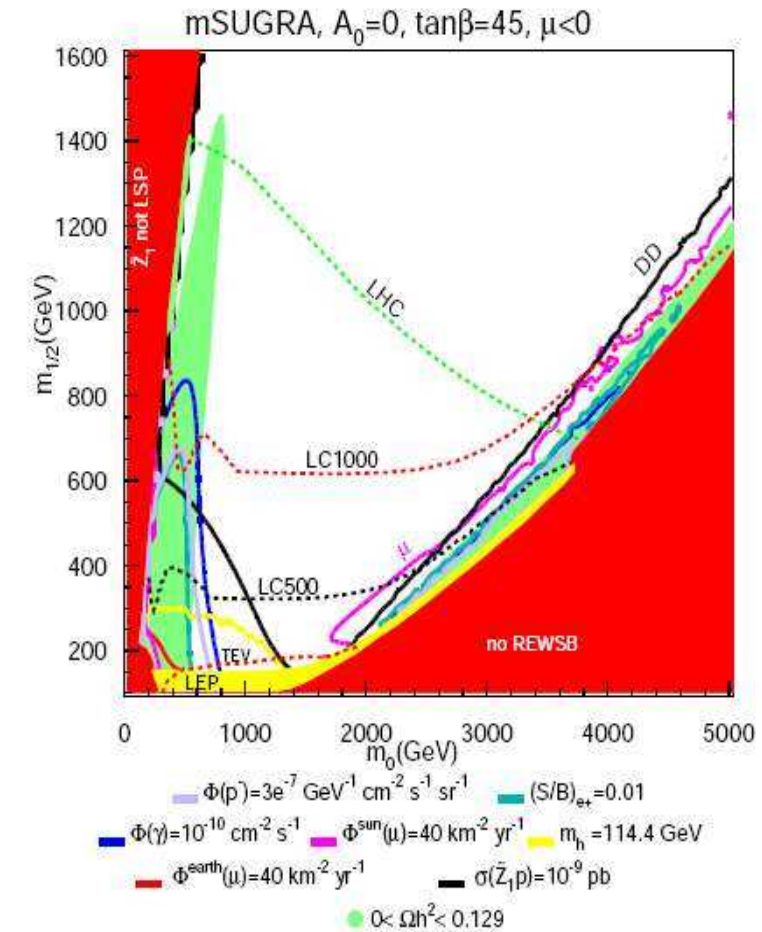
Outline

- Introduction
 - ★ Review of mSUGRA
 - ★ Motivations for SUSY models without universality in SSB terms
- Updated results on parameter space of mSUGRA
- Models with non-universal soft terms
 - ★ Non-universal scalar mass models
 - ★ Non-universal gaugino mass models
- Implications for collider searches
- Implications for direct and indirect dark matter detections
- Conclusions

Review of mSUGRA

- **Parameter space: universal SSB at $Q = M_{GUT}$**
 $m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
- From WMAP results, $\Omega_{CDM}h^2 = 0.111^{+0.011}_{-0.015}$
 (upper bound is a tight constraint on SUSY models containing DM candidates)
- **WMAP allowed Regions in m_0 - $m_{1/2}$ space**
 1. **$\tilde{\tau}$ co-annihilation region** at low m_0 , $m_{\tilde{\tau}_1} \sim m_{\tilde{Z}_1}$
 2. **bulk region** at low m_0 and $m_{1/2}$, light sleptons (LEP2 excluded)
 3. **Higgs-funnel H, A resonance** ($2m_{\tilde{Z}_1} \simeq m_{A,H}$) at large $\tan\beta \sim 50$ or h -resonance at low $m_{1/2}$ ($2m_{\tilde{Z}_1} \simeq m_h$)
 4. **FP/HB region** at large m_0 , low $\mu \rightarrow$ mixed higgsino dark matter (MHDM)

★ Region 1, 2, 3 \rightarrow Bino-like LSP



H.Baer et al. JCAP0408 (2004) 005

Motivations for SUSY models without universality in SSB terms

- ★ all relic-density-consistent regions in mSUGRA are near the edges of theoretically (or LEP2 experiment) excluded regions
- ★ need to examine how already drawn conclusions from the mSUGRA model are affected by relaxing the universality assumptions
- ★ within R -parity conserved neutralino dark matter assumption, WMAP value provides a strong constraint reducing model parameter space by one unit

We assume,

- MSSM is an effective theory between the weak and GUT scale
- R -parity is conserved
- Neutralino LSP
- (near)degeneracy of first and second generation of SSB sfermions \rightarrow FCNC suppressed
- CP-violating phases in SSB suppressed \rightarrow CP contribution of SUSY is small

Computational Tools are,

- all mass spectrum: ISAJET 7.76
- relic density, direct detection rates: IsaTools package (IsaReD, IsaReS)
- all indirect dark matter detection rates: DarkSUSY

Updated results on parameter space of mSUGRA 1

- parameter Space

$m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$

- varying m_t

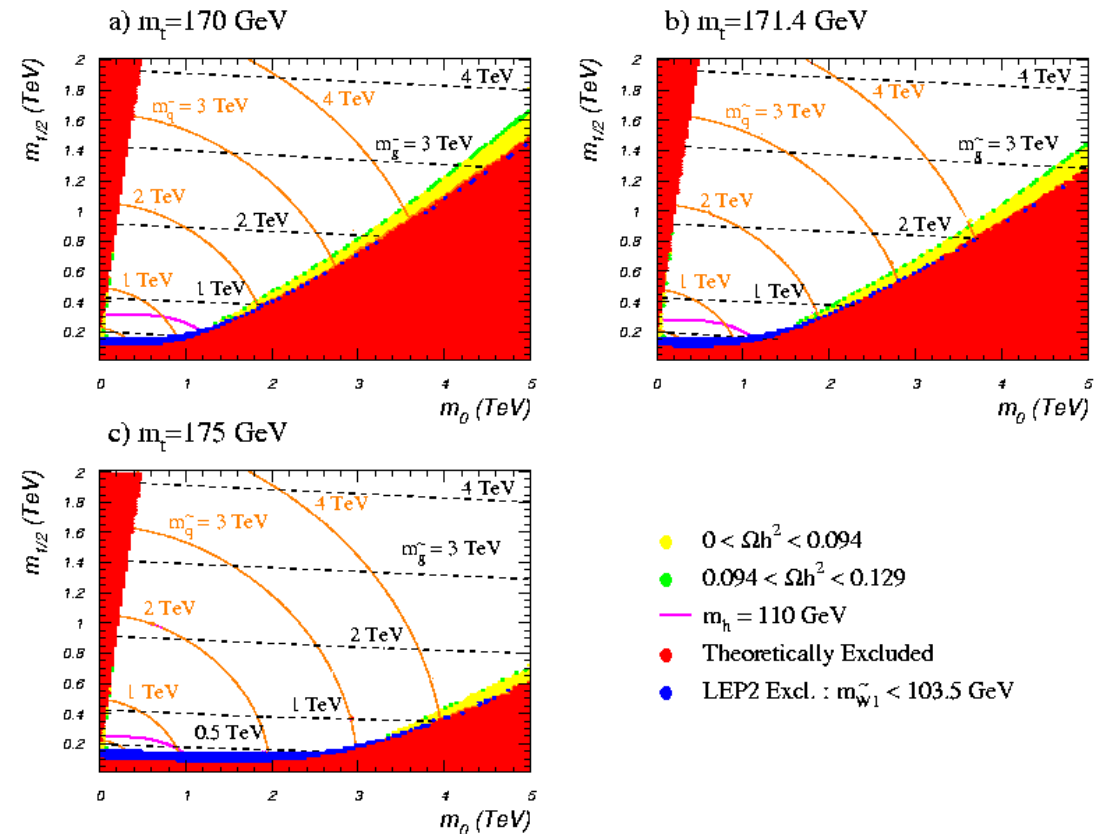
- location of EWSB excluded region

→ HB/FP region moves

- gluino and squark mass contours hardly change

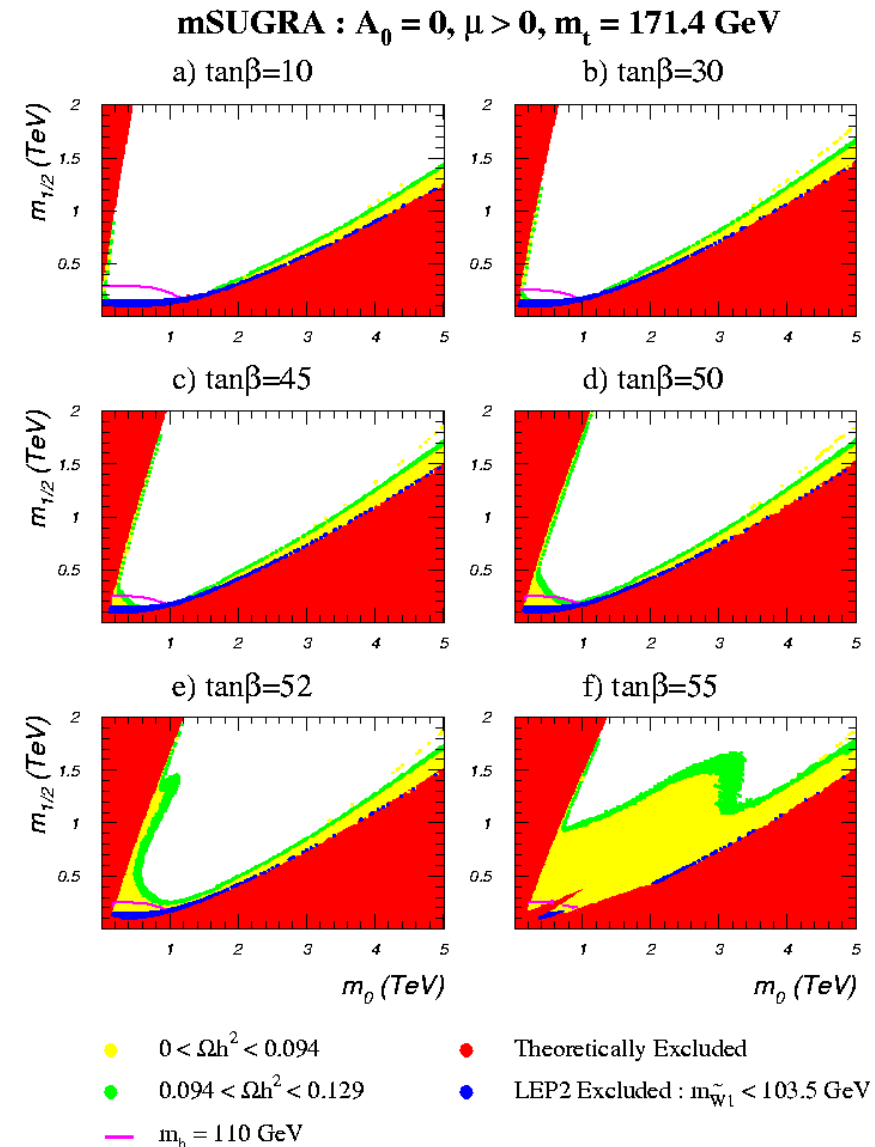
- as m_t increased, A -funnel moves to smaller m_0

mSUGRA : $\tan\beta=10, A_0=0, \mu>0$



Updated results on parameter space of mSUGRA 2

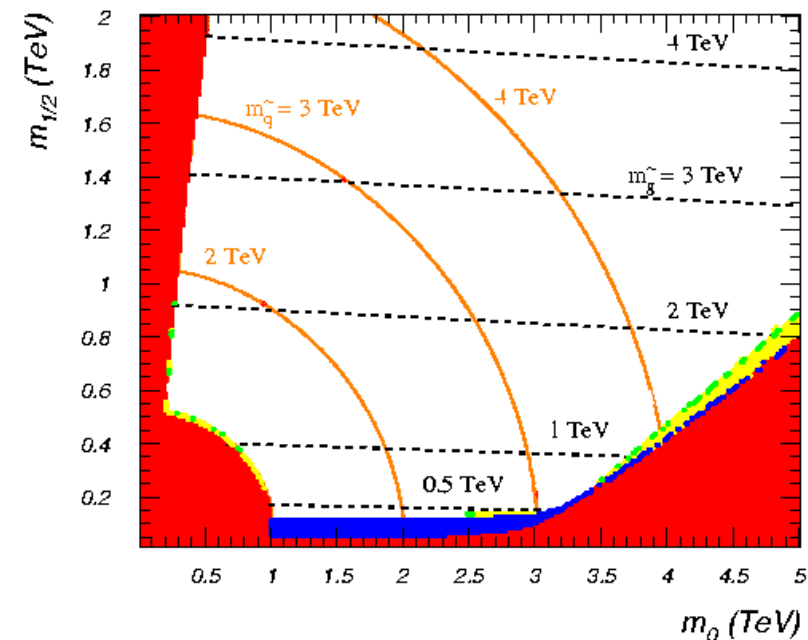
- **varying $\tan\beta$**
 - larger $\tan\beta$, wider WMAP allowed region
(as $\tan\beta$ grows, m_A drops due to b and τ Yukawa coupling effect)
 - as $\tan\beta$ increased, A -funnel moves to larger m_0
- **effect of $\mu < 0$**
 - A -funnel arises at lower $\tan\beta$
 - narrower A -funnel



Updated results on parameter space of mSUGRA 3

- effect of large negative A_0
 - reduce $m_{\tilde{t}_1}$
 - $\tilde{t}_1 - \tilde{Z}_1$ mass gap quite small
 - relic density reduced via stop co-annihilation

mSUGRA : $\tan\beta=10, A_0=-2 \text{ TeV}, \mu>0, m_t=171.4 \text{ GeV}$



- $0 < \Omega h^2 < 0.094$
- $0.094 < \Omega h^2 < 0.129$
- Theoretically Excluded
- LEP2 Excl. : $m_{\tilde{W}_1} < 103.5 \text{ GeV}$

Models with non-universal soft terms

- **Relic-density-consistent models** obtained by adjusting
 - composition of neutralino (**WTN**: Well-Tempered Neutralino^{*})
 *:Arkani-Hamed et al. Nucl.Phys.B741, 108, 2006
 - masses of neutralino or other sparticles
- **Non-universal scalar mass models**
 - Generation non-universality: Normal scalar mass hierarchy (NMH)
 - Non-universal Higgs mass: one extra parameter case (NUHM1 _{μ} , NUHM1_A)
 - non-universal Higgs mass: two extra parameter case (HS-Higgs Splitting)
- **Non-universal gaugino mass models**
 - Mixed Wino Dark Matter (MWDM)
 - Bino-Wino Co-Annihilation Scenario (BWCA)
 - Low $|M_3|$ Dark Matter: Compressed SUSY (LM3DM)
 - High $|M_2|$ Dark Matter: left-right split SUSY (HM2DM)
- Some benchmark cases with mSUGRA parameter space
 $m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu) = 300 \text{ GeV}, 300 \text{ GeV}, 0, 10, +1$ and $m_t = 171.4 \text{ GeV}$

Non-universal scalar mass models

- generation non-universality: Normal scalar Mass Hierarchy (**NMH**)
 $m_0(1, 2), m_0, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - $m_0(1, 2)$: first/second generation, $m_0(3) = m_{H_u} = m_{H_d} \equiv m_0$: remaining
 - dial $m_0(1, 2)$ to low enough to bulk (co-)annihilation via light sleptons
- non-universal Higgs mass: one extra parameter case (**NUHM1 $_{\mu}$** , **NUHM1 $_A$**)
 $m_0, \delta_\phi, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - $m_\phi = m_0(1 + \delta_\phi), m_{H_u}^2 = m_{H_d}^2 \equiv \text{sign}(m_\phi)|m_\phi|^2$
 - $m_\phi > m_0$: small μ and MHDM
 - $m_\phi < 0$: $m_A \sim 2m_{\tilde{Z}_1} \rightarrow$ at any $\tan\beta$
- non-universal Higgs mass: two extra parameter case (**HS-Higgs Splitting**)
 $m_0, m_{H_u}^2$ (equivalently μ), $m_{H_d}^2$ (equivalently m_A), $m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - $m_{H_{u,d}}^2 = m_0^2 (1 \mp \delta_H)$
 - $\delta_H < 0$: **low μ** and low m_A
 - $\delta_H > 0$: WMAP region via $\tilde{l}_L/\tilde{\nu}$ or \tilde{u}_R/\tilde{c}_R co-annihilation

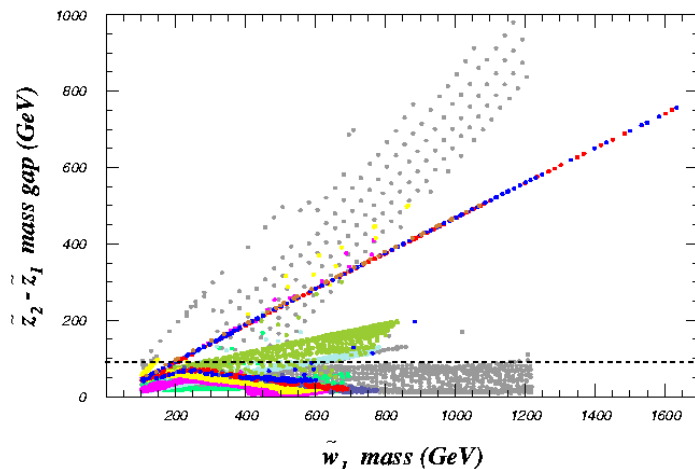
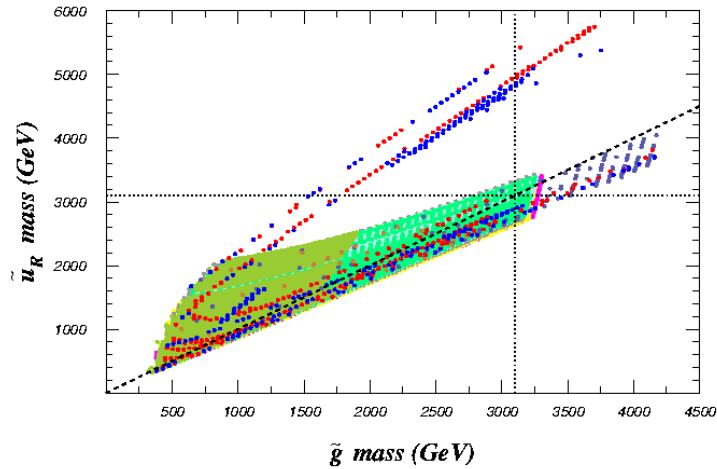
Non-universal gaugino mass models

- Mixed Wino Dark Matter (**MWDM1**, **MWDM2**):
 $m_0, M_1(\text{or } M_2), m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - by increasing the wino content of the LSP by reducing the ratio M_2/M_1
 - $M_1 \neq M_2 = M_3 = m_{1/2}$ or $M_2 \neq M_1 = M_3 = m_{1/2}$
- Bino-Wino Co-Annihilation Scenario (BWCA1, BWCA2):
 same as MWDM but M_1 and M_2 are in opposite sign
 - by allowing co-annihilation between high bino-like and wino-like states
- Low $|M_3|$ Dark Matter: Compressed SUSY (**LM3DM**):
 $m_0, M_3, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - by increasing the higgsino content of the LSP by decreasing the gluino mass
 - $M_3 \neq M_1 = M_2 = m_{1/2}$
- High $|M_2|$ Dark Matter: left-right split SUSY (**HM2DM**):
 $m_0, M_2, m_{1/2}, A_0, \tan\beta, \text{sign}(\mu)$
 - by allowing large M_2 mass
 - $M_2 \gg M_1 = M_3 = m_{1/2}$

Some Benchmark Cases: non-universal gaugino mass models

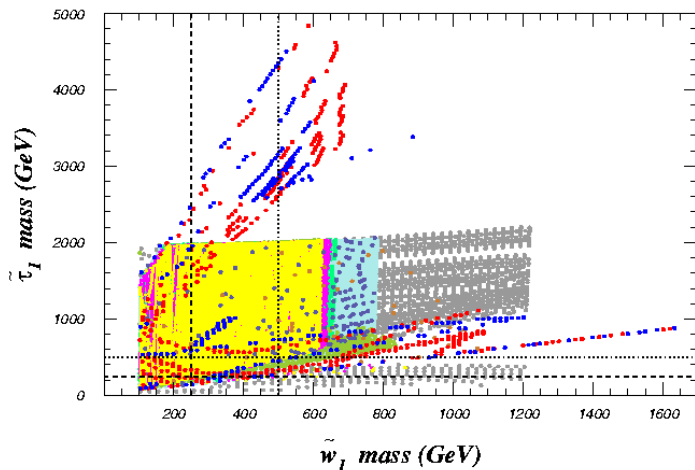
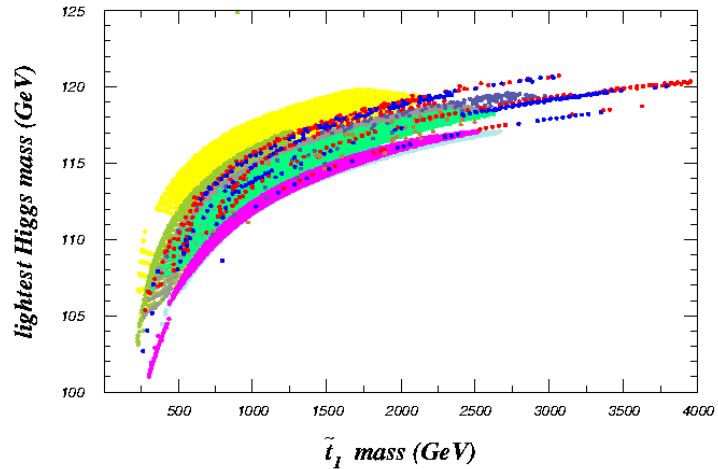
parameter	mSUGRA	MWDM	BWCA	LM3DM	HM2DM
special	—	$M_1(M_{GUT})$	$M_1(M_{GUT})$	$M_3(M_{GUT})$	$M_2(M_{GUT})$
value	—	490	-480	160	900
μ	385.1	385.9	376.6	185.3	134.8
$m_{\tilde{g}}$	729.7	729.9	731.7	420.2	736.4
$m_{\tilde{u}_L}$	720.8	721.2	722.0	496.9	901.8
$m_{\tilde{u}_R}$	702.7	708.9	709.9	467.0	696.3
$m_{\tilde{t}_1}$	523.4	526.5	536.3	312.2	394.3
$m_{\tilde{b}_1}$	656.8	656.0	658.9	443.2	686.4
$m_{\tilde{e}_L}$	364.5	371.5	371.4	366.1	669.3
$m_{\tilde{e}_R}$	322.3	353.3	352.2	322.6	321.3
$m_{\tilde{W}_2}$	411.7	412.4	404.5	282.9	719.7
$m_{\tilde{W}_1}$	220.7	220.8	220.0	152.5	136.5
$m_{\tilde{Z}_2}$	220.6	223.2	219.2	163.6	142.3
$m_{\tilde{Z}_1}$	119.2	194.6	201.7	105.5	94.8
m_A	520.3	525.9	518.6	398.3	670.7
m_{H^+}	529.8	535.3	528.1	408.7	679.8
m_h	110.1	110.2	109.8	106.0	111.9
$\Omega_{\tilde{Z}_1} h^2$	1.1	0.10	0.10	0.10	0.10
$\sigma_{SI}(\tilde{Z}_1 p)$	2.1×10^{-9} pb	1.5×10^{-8} pb	3.1×10^{-11} pb	7.2×10^{-8} pb	3.4×10^{-8} pb
$R_{\tilde{H}}$	0.15	0.25	0.16	0.50	0.67

Implications for collider searches 1



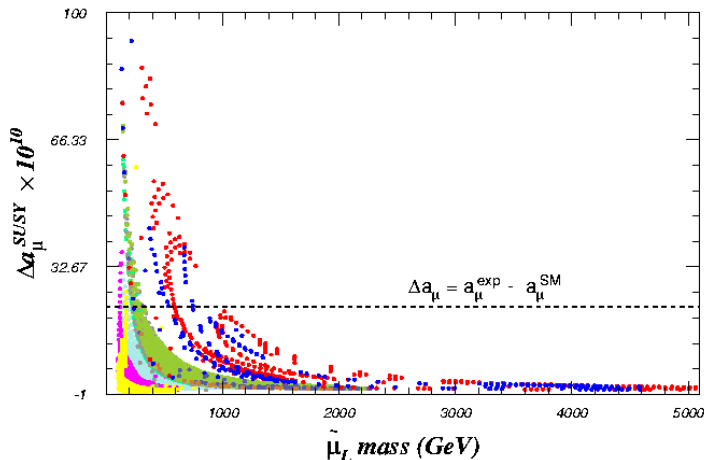
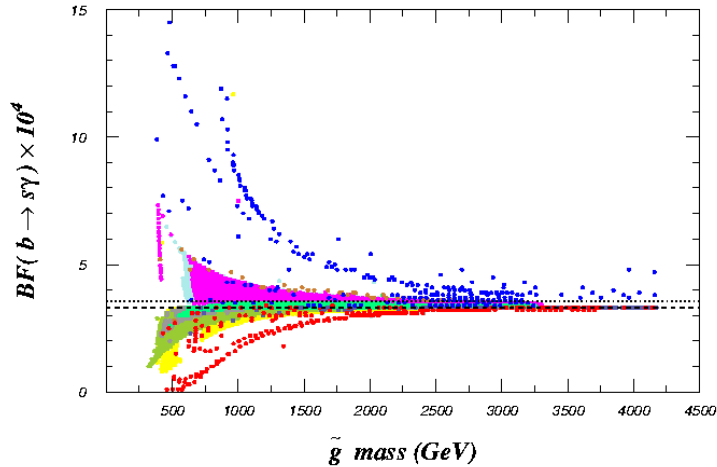
- – with $A_0 = 0$, $m_t = 171.4$ GeV, $\tan \beta = 10$
 (except for the mSUGRA model: $\tan \beta = 10, 30, 45, 50, 52$ and 55)
- non-universal mass dialed to yield $\Omega_{\tilde{Z}_1} h^2 \simeq 0.11$
- $m_{\tilde{g}}$ vs. $m_{\tilde{u}_R}$
 - dotted lines: 100 fb^{-1} reach of CERN LHC
 - dashed line: $m_{\tilde{u}_R} = m_{\tilde{g}}$
 - most of models within reach of LHC except HB/FP region of mSUGRA
- $m_{\tilde{W}_1}$ vs. $m_{\tilde{Z}_2} - m_{\tilde{Z}_1}$
 - dashed line: $m_{\tilde{Z}_2} - m_{\tilde{Z}_1} = M_Z$
 - below the line, 3-body decay like $\tilde{Z}_2 \rightarrow \tilde{Z}_1 l \bar{l}$ open
 - in most models, $m(l\bar{l})$ mass edge visible at LHC

Implications for collider searches 2



- m_h vs. $m_{\tilde{t}_1}$
 - heavier \tilde{t}_1 squarks are correlated with larger values of m_h (due to top-Yukawa radiative corrections to m_h)
 - in many models with $m_A \gg M_Z$, then $h \simeq H_{\text{SM}}$: the LEP2 lower bound of 114.1 GeV applicable
- $m_{\tilde{W}_1}$ vs. $m_{\tilde{\tau}_1}$
 - dashed lines: reach of ILC500 ($\sqrt{s} = 500$ GeV)
 - dotted lines: reach of ILC1000 ($\sqrt{s} = 1000$ GeV)

Implications for $BF(b \rightarrow s\gamma)$ and $(g - 2)_\mu$



- | | | |
|----------------------|---------|---------------------|
| • mSUGRA : $\mu > 0$ | • MWDM1 | • HM2DM : $M_2 > 0$ |
| • mSUGRA : $\mu < 0$ | • MWDM2 | • HM2DM : $M_2 < 0$ |
| • NUHM1 $_\mu$ | • BWCA2 | |
| • NUHM1 $_\Lambda$ | • LM3DM | |

- $BF(b \rightarrow s\gamma)$

- dotted line: combined experimental measurement (CLEO, Belle, BABAR)

$$BF(b \rightarrow s\gamma) = (3.55 \pm 0.26) \times 10^{-4}$$

- dashed line: SM prediction

$$BF(b \rightarrow s\gamma) = (3.15 \pm 0.23) \times 10^{-4}$$

- $(g - 2)_\mu$

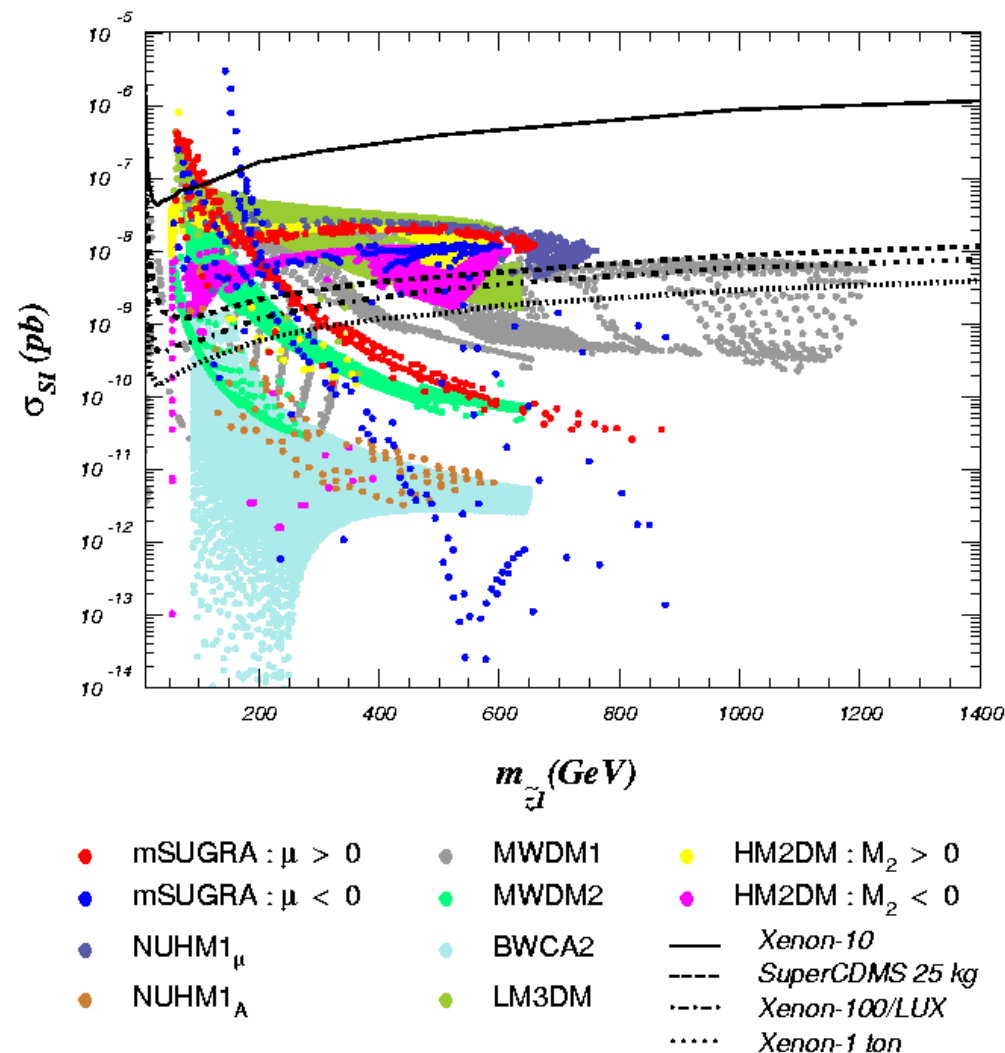
- positive deviation in $a_\mu \equiv \frac{(g-2)_\mu}{2}$

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 22(10) \times 10^{-10}$$

- $\Delta a_\mu^{\text{SUSY}} \propto \tan \beta$

Implications for direct dark matter detection

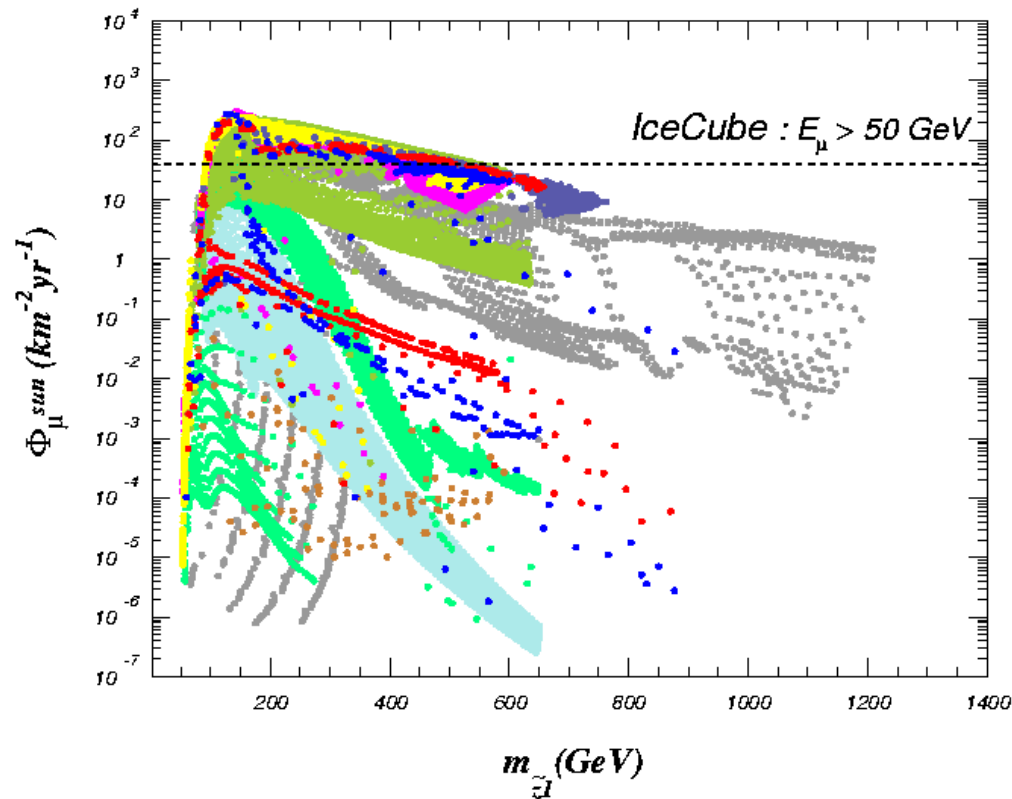
Spin-independent Direct Detection



- spin-independent neutralino-proton scattering cross section (with current and future experimental sensitivities: Xenon-10 (100, 1000), SuperCDMS, LUX)
- models with WTN within reach of next generation of detectors
- models adjusted masses to get WMAP value below sensitivities of detectors

Implications for indirect DM detection - Neutrino Detection

Neutrino Detection

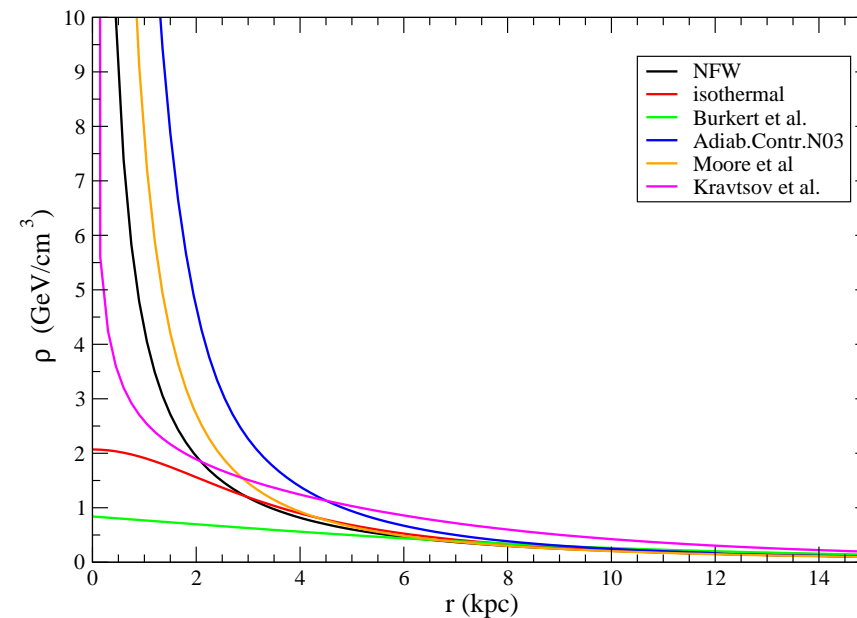


- | | | |
|----------------------|---------|---------------------|
| ● mSUGRA : $\mu > 0$ | ● MWDM1 | ● HM2DM : $M_2 > 0$ |
| ● mSUGRA : $\mu < 0$ | ● MWDM2 | ● HM2DM : $M_2 < 0$ |
| ● NUHM1 $_{\mu}$ | ● BWCA2 | |
| ● NUHM1 $_A$ | ● LM3DM | |

- Neutrinos from the Sun:
IceCube
- muon fluxes from neutralino annihilation in the solar core to ν_{μ} states
- main contribution comes from Z-exchange ← enhanced if neutralino has high higgsino content

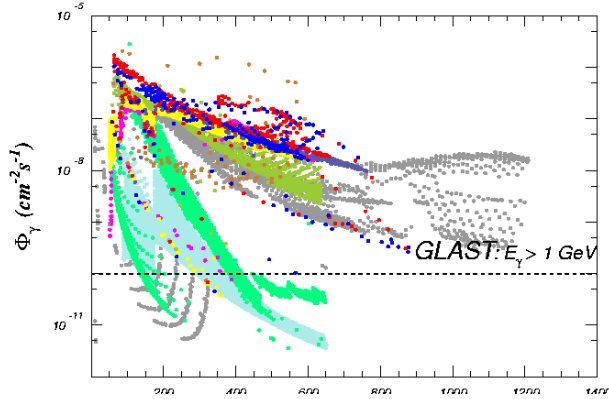
Implications for indirect(γ -ray, antiparticle) DM detection 1

- Detection of Gamma Rays from the galactic center: **GLAST**
- Detection of antiparticles:
 $\tilde{Z}_1 \tilde{Z}_1 \rightarrow W^+ W^-, q\bar{q}, ZZ, \dots \rightarrow jets$
 Antiprotons ($jets \ni \bar{p}$) : **PAMELA**
 Positrons ($jets \ni e^+$) : **PAMELA**
 Antideuterons ($jets \ni \bar{D}$) : **GAPS**
- High uncertainty from Halo Density Profile

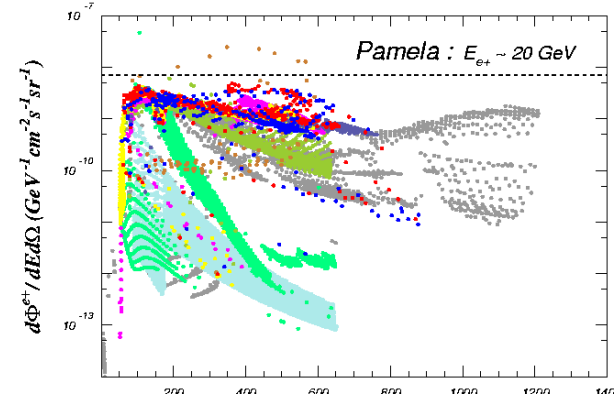


Implications for indirect(γ -ray, antiparticle) DM detection 2

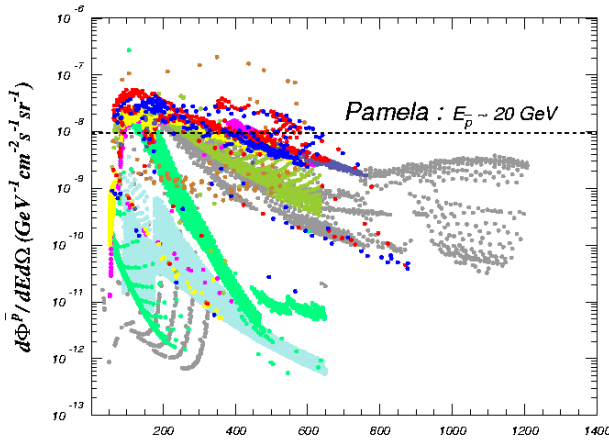
Gamma-ray Detection : Ad. Contr. N03 HM



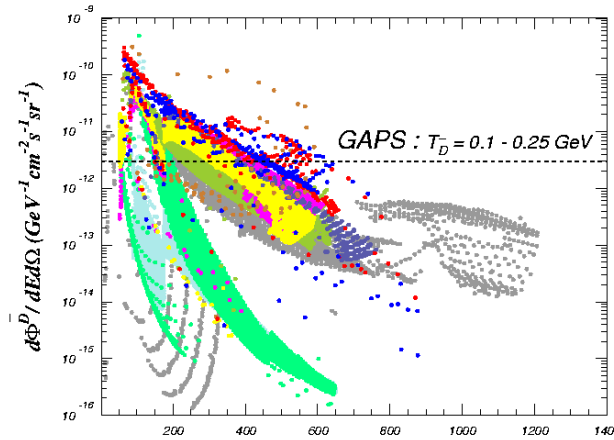
Positron Detection : Ad. Contr. N03 HM



Anti-proton Detection : Ad. Contr. N03 HM



Anti-deuteron Detection : Ad. Contr. N03 HM



- mSUGRA : $\mu > 0$
- mSUGRA : $\mu < 0$
- NUHM1 $_{\mu}$
- NUHM1 $_{\lambda}$
- MWDM1
- MWDM2
- BWCA2
- LM3DM
- HM2DM : $M_2 > 0$
- HM2DM : $M_2 < 0$

- mSUGRA : $\mu > 0$
- mSUGRA : $\mu < 0$
- NUHM1 $_{\mu}$
- NUHM1 $_{\lambda}$
- MWDM1
- MWDM2
- BWCA2
- LM3DM
- HM2DM : $M_2 > 0$
- HM2DM : $M_2 < 0$

Conclusions

1. ★ WTN occurs *only* in FP/HB region in mSUGRA (MHDM: $m_{\tilde{q}} \gg m_{\tilde{Z}_1, \tilde{W}_1, \tilde{g}}$).
 But, in relic-density-consistent models, easily get WTN with $m_{\tilde{q}} \sim m_{\tilde{g}}$
 ★ Higgs funnel enhancement is *only* for very large $\tan\beta$ values in mSUGRA.
 But, in non-universal Higgs mass models, we have Higgs funnel for any $\tan\beta$ value
2. In many relic-density-consistent models, $\tilde{Z}_2 - \tilde{Z}_1$ mass gap $< M_Z$
 → 2-body decay modes kinematically closed
 → 3-body decay modes open \Rightarrow at least one dilepton mass edge detectable at LHC
 → location of dilepton mass edge is clean signature of SUSY models
3. ★ $m_{\tilde{q}} = m_{\tilde{g}}, m_{\tilde{q}, \tilde{g}} < 3100$ GeV for most relic-density-consistent models
 → implies SUSY signals at LHC
 ★ $m_{\tilde{\tau}} < 500$ GeV for LM3DM
 → accessible at ILC with $\sqrt{s}=1$ TeV
4. In WTN models,
 ★ enhanced annihilation rates enhance direct DM detection rates
 ★ in many cases, muon neutrino signals accessible at IceCube
 ★ indirect DM searches in galactic halo into gamma rays and anti-matter elevated; large uncertainties associated with unknown galactic DM density profile

MSSM RGEs

$$\frac{dm_{H_u}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right)$$

$$\frac{dm_{H_d}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 - \frac{3}{10}g_1^2 S + 3f_b^2 X_b + f_\tau^2 X_\tau \right)$$

$$\frac{dm_{Q_3}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{1}{15}g_1^2 M_1^2 - 3g_2^2 M_2^2 - \frac{16}{3}g_3^2 M_3^2 + \frac{1}{10}g_1^2 S + f_t^2 X_t + f_b^2 X_b \right)$$

$$\frac{dm_{\tilde{t}_R}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{16}{15}g_1^2 M_1^2 - \frac{16}{3}g_3^2 M_3^2 - \frac{2}{5}g_1^2 S + 2f_t^2 X_t \right)$$

$$\frac{dm_{\tilde{b}_R}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{4}{15}g_1^2 M_1^2 - \frac{16}{3}g_3^2 M_3^2 + \frac{1}{5}g_1^2 S + 2f_b^2 X_b \right)$$

$$\frac{dm_{L_3}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 - \frac{3}{10}g_1^2 S + f_\tau^2 X_\tau \right)$$

$$\frac{dm_{\tilde{\tau}_R}^2}{dt} = \frac{2}{16\pi^2} \left(-\frac{12}{5}g_1^2 M_1^2 + \frac{3}{5}g_1^2 S + 2f_\tau^2 X_\tau \right)$$

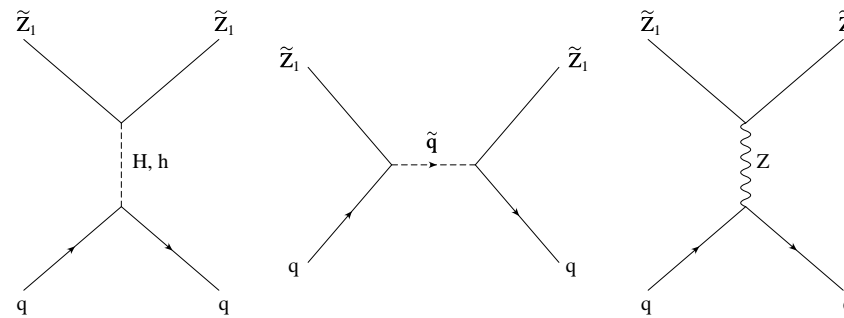
$$S = m_{H_u}^2 - m_{H_d}^2 + Tr \left[\mathbf{m}_Q^2 - \mathbf{m}_L^2 - 2\mathbf{m}_U^2 + \mathbf{m}_D^2 + \mathbf{m}_E^2 \right]$$

where $t = \log(Q)$, $f_{t,b,\tau}$ are the t , b and τ Yukawa couplings, and

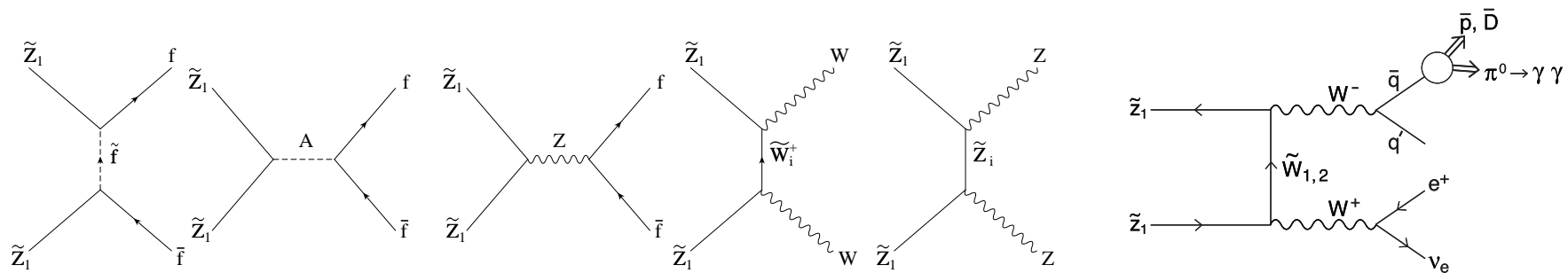
$$\begin{aligned} X_t &= m_{Q_3}^2 + m_{\tilde{t}_R}^2 + m_{H_u}^2 + A_t^2 \\ X_b &= m_{Q_3}^2 + m_{\tilde{b}_R}^2 + m_{H_d}^2 + A_b^2 \\ X_\tau &= m_{L_3}^2 + m_{\tilde{\tau}_R}^2 + m_{H_d}^2 + A_\tau^2 \end{aligned}$$

Feynman Diagrams Contributing to Neutralino DM Detection

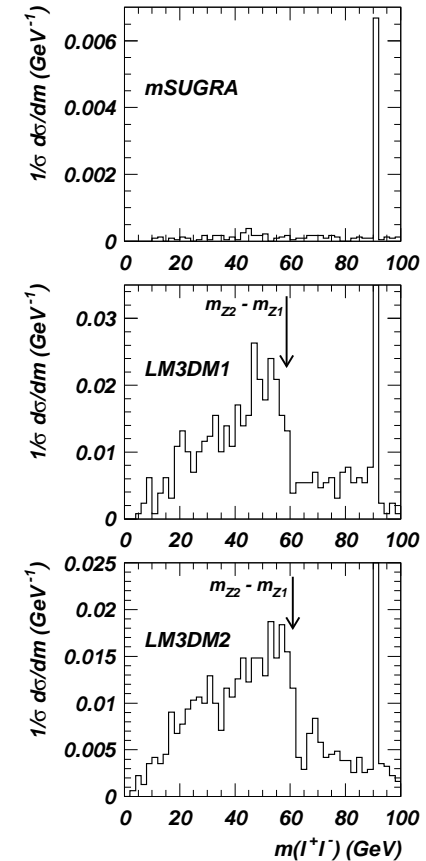
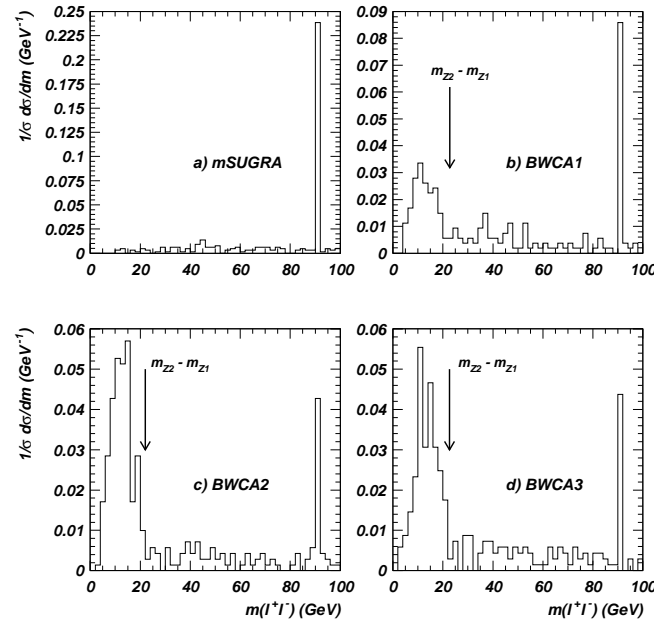
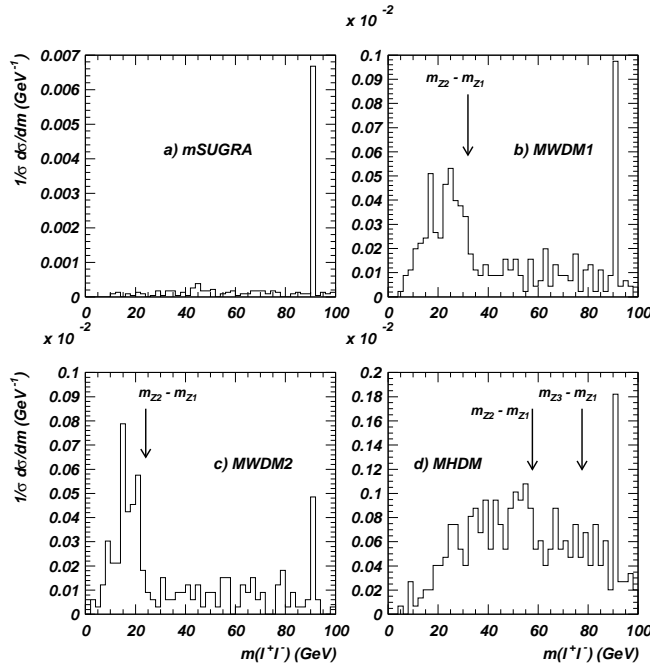
- Direct Detection



- Indirect Detection



Dilepton Distribution at LHC



- $E_T^{miss} > \max(100\text{GeV}, M_{eff})$, $E_T > 50\text{GeV}$ ($n_{jet} \geq 4$, hardest jet has $E_T > 100\text{GeV}$), $S_T > 0.2$, $M_{eff} > 800\text{GeV}$ LHC Point 5 from [PRD 55 \(1997\) 5520](#), [PRD 60 \(1999\) 095002](#)
- mSUGRA : sharp peak at $m(l^+l^-) \sim M_Z$ from $\tilde{Z}_2 \longrightarrow \tilde{Z}_1 Z^0$ decays
- NUGM :
 Z^0 peak from $\tilde{Z}_3, \tilde{Z}_4, \tilde{W}_2$ decays + continuum distribution $m(l^+l^-) < m_{\tilde{Z}_2} - m_{\tilde{Z}_1}$